

THE CARINA PROJECT VII: TOWARDS THE BREAKING OF THE AGE-METALLICITY DEGENERACY OF RED GIANT BRANCH STARS USING THE $C_{U,B,I}$ INDEX

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ABSTRACT

We present an analysis of photometric and spectroscopic data of the Carina dSph galaxy, testing a new approach similar to that used to disentangle multiple populations in Galactic globular clusters (GCs). We show that a proper colour combination is able to separate a significant fraction of the red giant branch (RGB) of the two main Carina populations (the old one, ~ 12 Gyr, and the intermediate-age one, 4–8 Gyr). In particular, the $C_{U,B,I} = (U - B) - (B - I)$ pseudo-colour allows us to follow the RGB of both populations along a relevant portion of the RGB. We find that the oldest stars have more negative $C_{U,B,I}$ pseudo-colour than intermediate-age ones. We correlate the pseudo-colour of RGB stars with their chemical properties, finding a significant trend between the iron content and the $C_{U,B,I}$. Stars belonging to the old population are systematically more metal poor ($[Fe/H] = -2.32 \pm 0.08$ dex) than the intermediate-age ones ($[Fe/H] = -1.82 \pm 0.03$ dex). This gives solid evidence on the chemical evolution history of this galaxy, and we have a new diagnostic that can allow us to break the age-metallicity degeneracy of H-burning advanced evolutionary phases. We compared the distribution of stars in the $C_{U,B,I}$ plane with theoretical isochrones, finding that no satisfactory agreement can be reached with models developed in a theoretical framework based on standard heavy element distributions. Finally, we discuss possible systematic differences when compared with multiple populations in GCs.

Subject headings: (galaxies:) Local Group; Galaxies: individual: Carina dSph; Galaxies: abundances; Techniques: photometric; Techniques: spectroscopic;

1. INTRODUCTION

The classical question of how galaxies in general formed and evolved is one that can be illuminated by the study of galaxies in the Local Group (LG). Particularly the numerous dwarf galaxies that are thought in some respects (mass, low metals) to be similar to the building blocks that have and are still being accreted by more massive galaxies such as our own Galaxy and M31. The characterization of the resolved stellar populations in terms of age and chemical content of dwarf galaxies in the LG has been the target

of large observational efforts in the last decades (e.g. Gallart et al. 1996; Gallagher et al. 1998; Held et al. 1999; Aparicio et al. 2001; Bellazzini et al. 2001; Carrera et al. 2002; Dolphin et al. 2001; Skillman et al. 2003; Momany et al. 2005; McConnachie & Irwin 2006; Cole et al. 2007; Rizzi et al. 2007; Walker et al. 2009; Martin et al. 2009; Monelli et al. 2010a,b; Sanna et al. 2010; Hidalgo et al. 2011; Battaglia et al. 2012a; Dall'Orta et al. 2012; de Boer et al. 2012; Okamoto et al. 2012).

Until recently, dwarf galaxies were thought to be fundamentally different from globular clusters (GCs). However, the recognition that many, if not all, GCs contain multiple populations (Kraft et al. 1992; Cannon et al. 1998; Grundahl et al. 1999; Bedin et al. 2004; Marino et al. 2008; Milone et al. 2008; Yong & Grundahl 2008; Lee et al. 2009; Piotto et al. 2012; Monelli et al. 2013) and that some of the most massive clusters may be the remnants of dissipated dwarf galaxies (Bekki et al. 2007) has blurred the differences somewhat. When considering the build-up of the halo of our own Galaxy, its chemical evolution is likely to be intimately intertwined with that of the GCs and accreting dwarf galaxies. The first high resolution spectra for a handful of stars in nearby dSphs (Shetrone et al. 2001, 2003; Tolstoy et al. 2003) disclosed a systematic difference in the chemical enrichment law compared to the halo stars. This implies that the building blocks of the halo can not resemble the *present day* Galaxy satellites, unless the merging events occurred very early on, before the internal chemical evolution driven by

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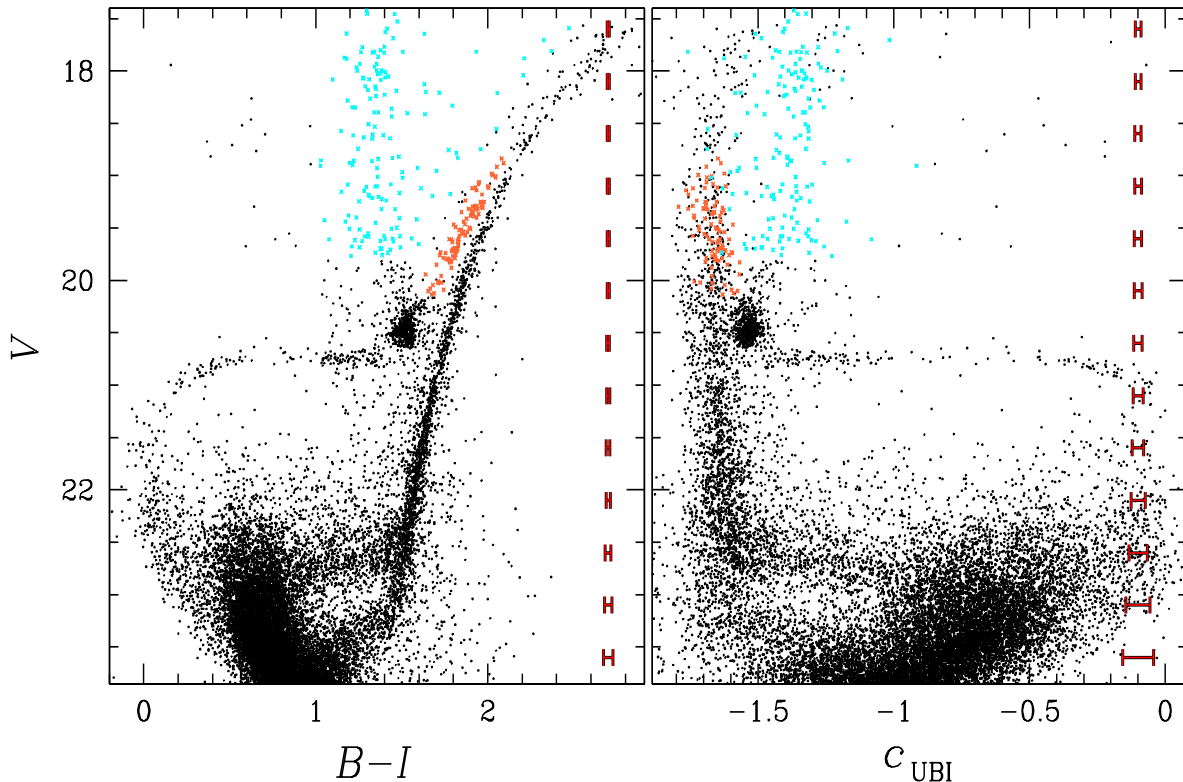


FIG. 1.— *Left* - $(V, B-I)$ CMD of Carina stars, based on the photometry presented in Bono et al. (2010). Bright field stars are highlighted in cyan, while orange symbols show the Carina AGB stars; *Right* - $(V, c_{U,B,I})$ plane, where the RGBs of the old and intermediate-age populations largely split.

Supernova enrichment took place. On the other hand, it has recently been suggested that GCs might be responsible for a significant fraction of the halo stars observed today (D’Ercole et al. 2008). In this scenario, the GCs formed two or more generations of stars, on a short time scale, of the order of few hundred Myr, and the first Supernovae would be responsible for a significant mass loss from the clusters, causing the evaporation of a large fraction of the first generation stars; these would build up part of the Galaxy halo. Hence, a detailed knowledge of the chemical evolution of nearby dwarfs and a comparison with GCs can give important insight on the progenitors of our own Galaxy.

Ideally, we would like to collect high resolution spectroscopy for large samples of stars to faint magnitudes in conjunction with accurate photometry. However for LG galaxies the former is technically at present beyond our means and only typically the brightest stars in the closer galaxies have such data. Deep photometry alone suffers from the long-standing problem of the photometric colour-magnitude diagram (CMD) having an age-metallicity degeneracy that affects the advanced evolutionary phases such as the red giant branch (RGB), where sequences of different age-metallicity combinations occupy the same region of the CMD and therefore can not be easily disentangled.

Interestingly, recent results revealed that the different stellar populations in old GCs can be easily isolated along the whole CMD, from the main sequence (MS), up to the subgiant branch (SGB), RGB, and even the horizontal

branch by using an appropriate combination of broad band filters (Marino et al. 2008; Sbordone et al. 2011; Milone et al. 2012b). Monelli et al. (2013)¹² showed that the $c_{U,B,I} = (U - B) - (B - I)$ index is a powerful tool to identify multiple stellar sequences in the RGB of old GCs, and that the $c_{U,B,I}$ pseudo-colour of RGB stars correlates with the chemical abundances of light elements.

In this paper we test the same approach successfully used for GCs for the first time in a dwarf galaxy. Since the established nomenclature can be somehow confusing, it has to be clearly stated that when we refer the stellar populations in a dwarf galaxy, in particular the dSph satellites of the Milky Way, these have substantially different properties from multiple populations in GCs. First, the typical main star formation event in a dwarf galaxy occurred on time scales of the order of few Gyr, significantly longer than the age difference between two generations of stars in a GC (few hundred Myr at most). Moreover, the chemical evolution is different. In particular, the large spread in Fe observed in dwarf galaxies has no counterpart in a typical GC. In these systems, the internal chemical enrichment affected only the light elements involved in the high temperature H burning processes, while typically no spread in Fe, is found.

In this paper we focus on the properties of stellar population in the Carina dSph, for which an extensive database of both photometric (Bono et al. 2010;

¹² <http://www.iac.es/project/sumo>

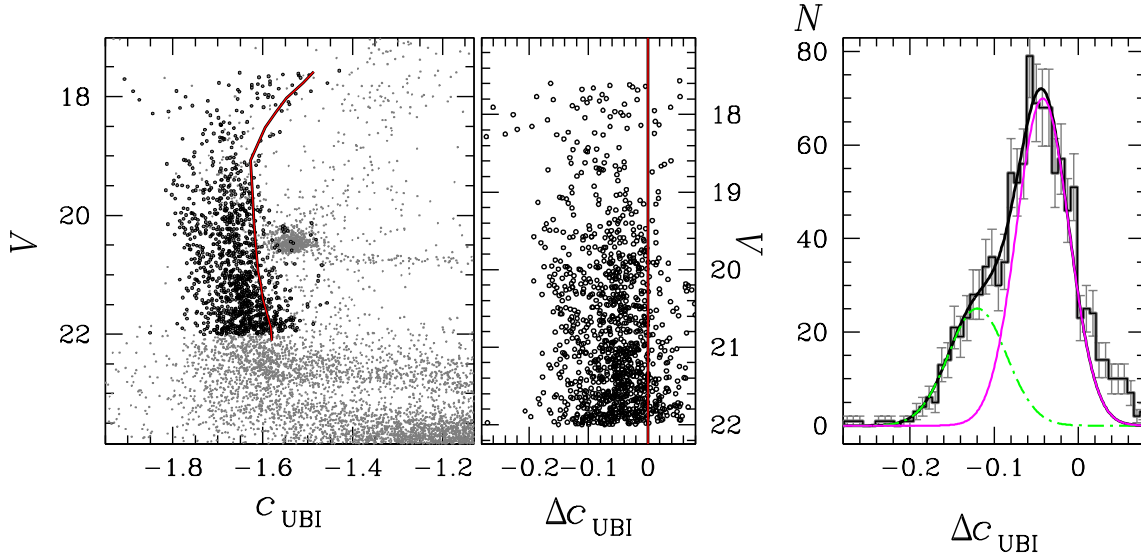


FIG. 2.— *Left*) The sample of RGB stars adopted to identify substructures in the RGB of Carina are shown as black open circles (1134 stars). The red line shows our adopted right envelope of the sequence. *Center* - the Carina RGBs, rectified to the red line. For each star we display the $\Delta c_{U,B,I}$ index, the colour difference with respect to the reference red line. *Right* - Histogram of $\Delta c_{U,B,I}$, with gaussian kernels superimposed. The overall distribution can be well represented by two gaussian components.

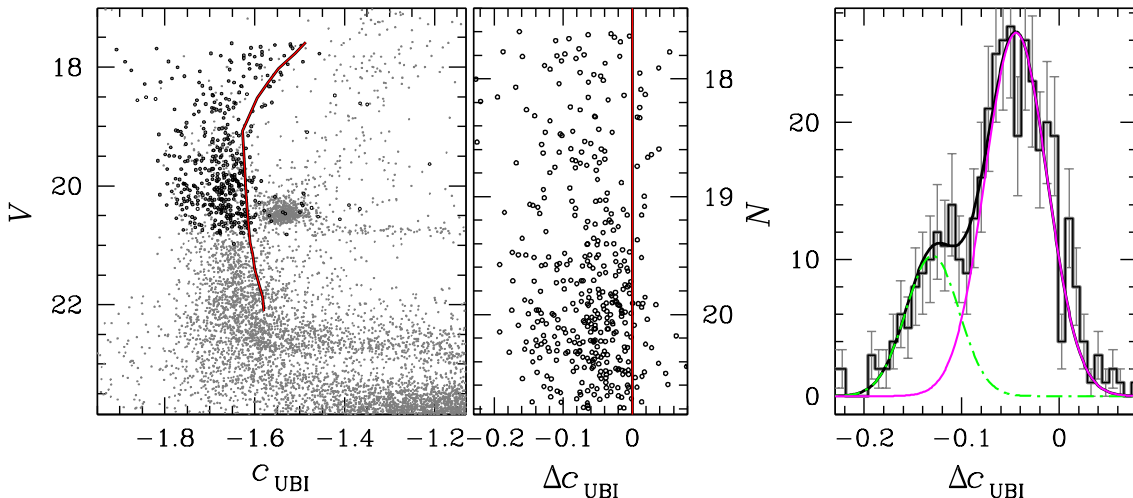


FIG. 3.— Same as Figure 2, but in this case the open circles in the left panel mark 413 RGB stars with radial velocity consistent with that of Carina, selected from the sample of Fabrizio et al. (2011). In the right panel, the presence of a double peak in the $\Delta c_{U,B,I}$ distribution is confirmed.

Battaglia et al. 2012b) and spectroscopic (Koch et al. 2006; Helmi et al. 2006; Fabrizio et al. 2011, 2012; Venn et al. 2012; Lemasle et al. 2012) data is available. Nevertheless, we still lack a definitive understanding of its bursty star formation history (Smecker-Hane et al. 1996; Monelli et al. 2003; Stetson et al. 2011), unique in the Local Group, and of the chemical enrichment history of its different stellar populations. In fact, accurate analysis of high-quality photometry revealed that Carina experienced two main events of star formation, separated by a quiescent phase lasting few Gyr, which produced two well separated SGBs. One corresponds to an old population (>10 Gyr) containing approximately one third of the total number of stars, while the second belongs to an intermediate-age population made of ~ 4 -

8 Gyr-old stars (Smecker-Hane et al. 1996; Monelli et al. 2003). The two SGBs merge in a narrow RGB, making it difficult to associate the individual iron abundances with the discrete SGB and main sequence (Koch et al. 2006; Fabrizio et al. 2012; Venn et al. 2012), observed in the CMD. This represents a major challenge to understanding the complex star formation history and the chemical evolution of the Carina dSph.

The paper is organized as follows. In section 2 we present the $c_{U,B,I}$ diagram for Carina, and the correlation between the $c_{U,B,I}$ pseudo-colour and the Fe content of RGB stars. In section 3 we discuss the properties of Carina's stars with theoretical isochrones and GCs. The conclusions in Section 4 close the paper.

2. DATA ANALYSIS

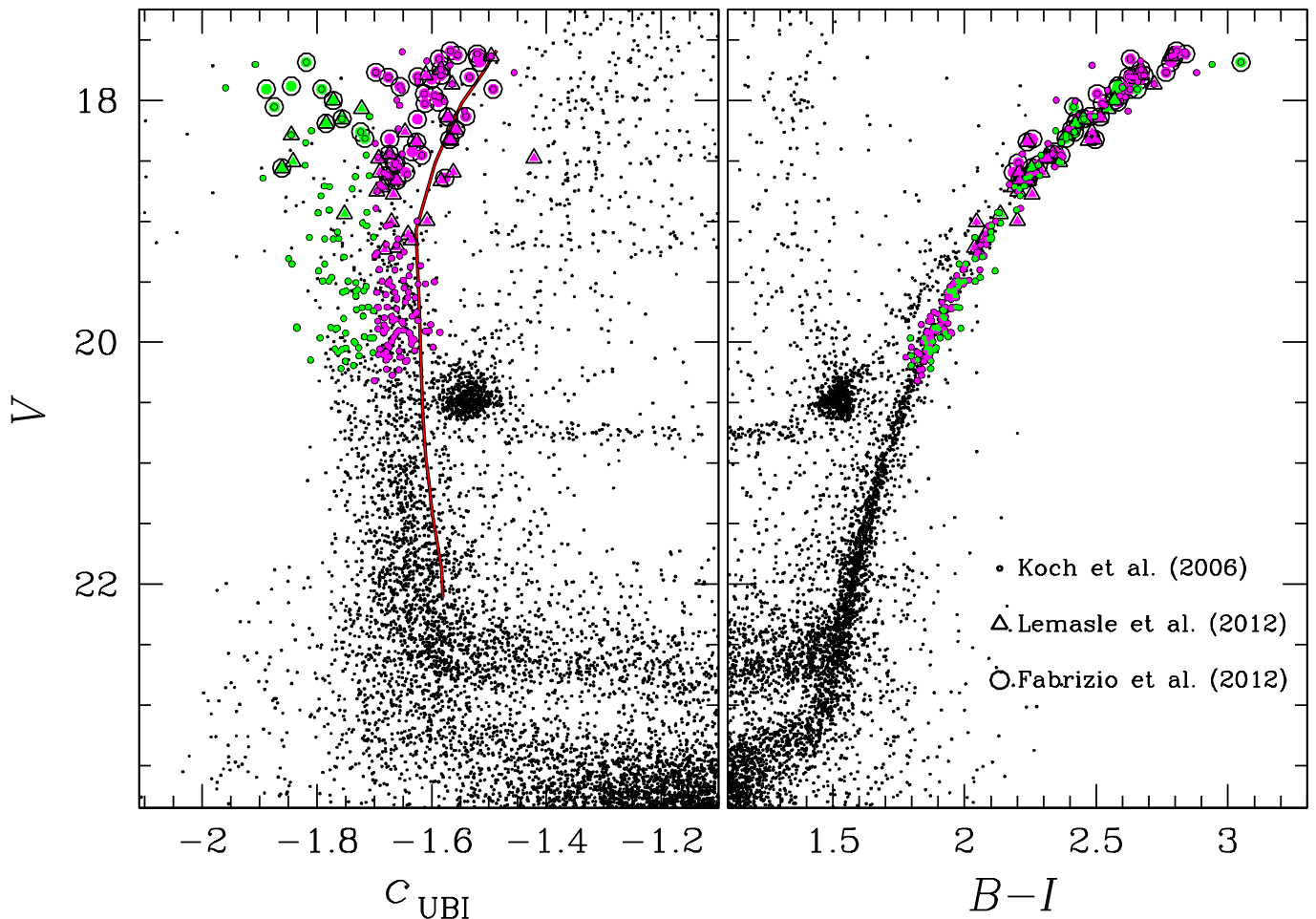


FIG. 4.— *Left* - (V , $c_{U,B,I}$) pseudo-CMD with superimposed the stars for which spectroscopic measurements are available. Large symbols show stars with available Fe abundances from high-resolution spectra (dots: Fabrizio et al. 2012; triangles: Lemasle et al. 2012). Small coloured dots mark the 212 stars selected from Koch et al. (2006), for which the Fe abundance was derived from CaT measurements. Green and magenta symbols indicate stars with $c_{U,B,I} < -1.70$ mag and $c_{U,B,I} > -1.70$ mag, respectively. *Right* - (V , $B-I$) CMD showing the complete degeneracy of spectroscopic targets on the RGB, using the same colour coding.

2.1. Photometric data: splitting the Carina RGB

The photometric data are the same already presented in Bono et al. (2010). In particular, we focus here on the central region only, where U, B, V , and I data overlap over an area of $\approx 40' \times 40'$. The left panel of Figure 1 shows the (V , $B-I$) CMD of 20,240 stars selected with the following criteria: *i*) they are measured in the four bands; and *ii*) they are bona-fide Carina stars, with removal of most of the possible Galactic field stars and foreground galaxies following the procedure explained in Bono et al. (2010), and based on the position of the sources in the ($U-V$), ($B-I$) colour-colour plane. The plot demonstrates a nicely cleaned CMD showing well-defined evolutionary sequences, in particular, the two well separated turn-offs and SGBs representing the old and intermediate-age populations, merging into the thin

RGB. The few remaining field stars populate an almost vertical sequence at colour $1.2 < (B-I) < 1.6$ mag (cyan symbols for the brightest ones). These stars are virtually impossible to clean even using a colour-colour plane, because their position is almost indistinguishable from the Carina TO stars. Note that most of the stars bluer than the field sequence and brighter than $V = 20$ mag are Anomalous Cepheids of Carina (Coppola et al. 2013). The orange crosses mark the faint part of the asymptotic giant branch (AGB) stars sequence.

The right panel of the same figure shows the (V , $c_{U,B,I}$) pseudo-CMD of Carina. As discussed in detail by Monelli et al. (2013), the features in the (V , $c_{U,B,I}$) diagram are reversed compared to a standard CMD, at least in the metallicity range covered by the Carina stars. The $c_{U,B,I}$ of MS stars gets larger (i.e., less negative) as the stars get brighter, and after the turn-off the stars evolve

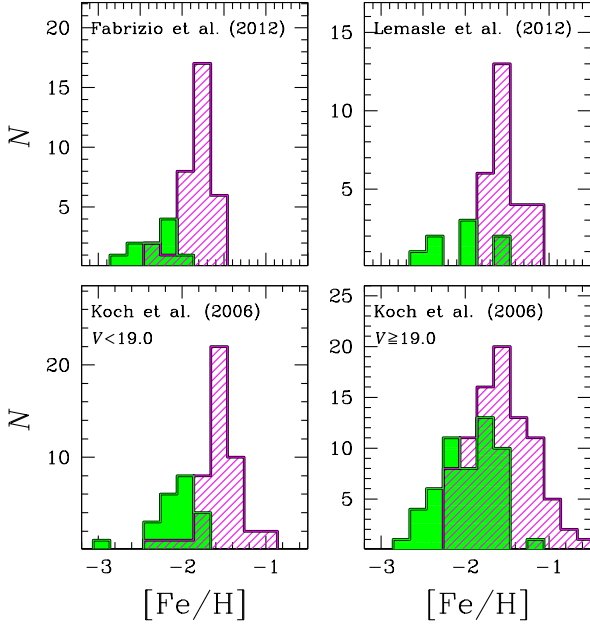


FIG. 5.— The metallicity distribution of the three spectroscopic samples. The top panels show the high-resolution samples: Fabrizio et al. (2012, 44 stars, left) and Lemasle et al. (2012, 35 stars, right). In the lower panels, the medium-resolution sample from Koch et al. (2006) was split in two subgroups: stars with $V < 19$ mag (71, bottom left), and stars with $V \geq 19$ mag (141, bottom right).

to lower index values along the two SGBs. In this plane the two RGBs do not totally merge in a single, narrow sequence, as happens in standard optical CMDs. Although some degree of overlap is present for $-1.70 < c_{U,B,I} < -1.6$ mag, it is possible to follow the two RGB sequences which remain well-defined, and run almost vertically and parallel from the SGB to the tip of the RGB. In particular, the RGB stars with more negative $c_{U,B,I}$ are a sequitur of the SGB of the old population, while the more densely populated, higher $c_{U,B,I}$ side of the RGB is the sequitur of the intermediate-age population. Only at the brightest magnitudes ($V \lesssim 19$ mag) the two sequences diverge slightly. We stress that the photometric error is of the order of few hundredths of magnitude along the whole RGB, and therefore cannot account for the observed spread in the $c_{U,B,I}$ index. Note that the contamination due to field stars is negligible across the RGB, while in this plane the majority of AGB stars overlie the RGB sequences. For this reason, the latter have been removed from the following analysis.

To better characterize these two RGB sequences, we followed the procedure outlined in Figure 2. Bona-fide RGB stars are shown as black open circles (left and central panels), while the red line, drawn by eye, is intended to represent the right edge of their distribution. Our selection includes only stars in the magnitude range $17.5 < V < 22$ mag. Nevertheless, we verified that the following analysis is minimally affected, within 1σ , by both the exact location of the envelope and the limit magnitude. The RGB was rectified with respect to the red line, which is the origin of the abscissas in the central panel. This shows, for each star, the distance in colour $\Delta c_{U,B,I}$ from the red line. Finally, the right panel presents the distribution of the $\Delta c_{U,B,I}$ (grey histogram).

The shape of the global distribution is best fitted by the sum (black line) of the two superimposed gaussian curves (green and magenta lines), whose peaks are separated by ~ 0.08 mag. This indicates that a simple photometric index such as the $c_{U,B,I}$ is able to largely separate, for the first time, the two main components along the RGB of Carina. In particular, we conclude that stars with $c_{U,B,I} < -1.70$ mag, belong to the old population, while stars with less negative index values are predominantly intermediate-age.

We verified this finding by considering only kinematically selected stars, adopting the sample of RGB stars from Fabrizio et al. (2011). This is shown in Figure 3, which is a replica of Figure 2 with superimposed 413 RGB stars with radial velocity consistent with that of Carina. By adopting the selection from Fabrizio et al. (2011) and retaining stars with radial velocities within 4σ from the mean value, in the range $+180$ to $+260$ km s^{-1} , the occurrence of a double peak in the pseudo-colour distribution due to the two main Carina populations is confirmed.

2.2. Spectroscopic data: connecting multiple sequences and metallicity

In this section, we investigate whether a connection exists between the two sequences identified in the RGB and the chemical compositions of member stars. To do this, we use three independent samples of spectroscopic data available in the literature (see Figure 6). We adopt two samples of high-resolution measurements of Fe lines, from Fabrizio et al. (2012, $R \sim 40,000$, large circles) and Lemasle et al. (2012, $R \sim 22,000$, triangles). The two samples include 44 and 35 stars for a total of 68 red giants (11 in common). The entire sample of stars with high-resolution spectra has at least one photometric measurement in the four adopted filters, namely V , and UBI (see Fig. 6). We also included red giant stars for which Fe abundances were determined by Koch et al. (2006) using medium-resolution ($R \sim 6000$) spectra (small circles in Fig. 6) in the CaT region. Out of the initial catalogue by Koch et al. (2006, see their Tab. 6), including 1,197 stars, we selected 212 objects with $[Fe/H]$ abundance and obeying to the same photometric and radial velocity selection criteria adopted in Fig. 1 and Fig. 2. We note that in this analysis, we adopt the $[Fe/H]$ abundance from Koch et al. (2006), and the radial velocity from Fabrizio et al. (2011).

The analysis was performed splitting all the spectroscopic samples according to their $c_{U,B,I}$ index. In particular, green and magenta symbols account for stars with $c_{U,B,I} < -1.70$ mag and $c_{U,B,I} > -1.70$ mag, respectively. For comparison, the right panel presents the $(V, B - I)$ classical CMD, where the two samples of stars selected according the $c_{U,B,I}$ index are mixed. Figure 6 presents the metallicity distribution for the three samples. The sample from Koch et al. (2006) has been further split in two, separating the brightest (bottom left, $V < 19$ mag, 71 stars) from the faintest (bottom right, $V \geq 19$ mag, 141 stars) ones, to account for the change in the RGB morphology previously discussed (Figure 1). The plot discloses that the stars selected on the sequence with more negative $c_{U,B,I}$ (green histogram), identified as the RGB of the old population, are on average more metal-poor than the stars on the other sequence (magenta),

dominated by the intermediate-age population. The different, independent samples provide a very good overall agreement, and in particular the sample of bright stars from Koch et al. (2006) notably agree with the high-resolution samples. In the case of the faint CaT stars, the overlap between the two histogram increases, possibly due to the increase in the observational errors. The mean metallicity of each sample is reported in Table 1. We find that the mean metallicity of the old population is ≈ 0.5 dex more metal-poor than the intermediate-age one¹³. Assuming the Fabrizio et al. (2012) data, which include stars with both FeI and FeII measurements, we find that the mean metallicities are $[\text{Fe}/\text{H}] = -2.32 \pm 0.08$ dex and $[\text{Fe}/\text{H}] = -1.82 \pm 0.04$ dex for the old and the intermediate-age group, respectively. While previous investigations (see e.g. Lemasle et al. 2012) have suggested a similar chemical evolution for Carina, we stress that our approach is independent of isochrone fitting. The identification of RGB stars as members of the old or the intermediate-age population does not require previous knowledge of the metallicity.

The cut adopted to split the two quoted populations ($c_{\text{U,B,I}} = -1.73$) mag is, as noted by the anonymous referee, arbitrary. Mild changes in the adopted cut can move objects from the old sample into the intermediate-age one and viceversa. To constrain on a quantitative basis the impact of the adopted cut on the mean metallicity of the two samples, we performed the selection by adopting $c_{\text{U,B,I}} = -1.67$ and $c_{\text{U,B,I}} = -1.73$ mag. The difference was fixed according to the photometric error of the $c_{\text{U,B,I}}$ index at $V \sim 20.5$ ($\sigma_{\text{UBI}} = 0.03$ mag). The mean metallicities listed in Table 1 further support that the criterium adopted to split the two samples minimally affect the current conclusions. In particular, the systematic difference between the mean metallicity of the old and the intermediate-age population is systematically, on average, larger than 0.5 dex. This result is an independent demonstration that the colour spread observed in $c_{\text{U,B,I}}$ is intrinsic. In fact, the $c_{\text{U,B,I}}$ index and the metallicity used here have been measured in an independent way. If the RGB spread observed in $c_{\text{U,B,I}}$ was entirely due to photometric errors (either statistical or systematic), a star with small (large) $c_{\text{U,B,I}}$ would have the same probability of being either metal-rich or metal-poor. Moreover, this result is supported by three independent sets of spectroscopic measurements.

Figure 6 presents the iron abundance as a function of the $\Delta c_{\text{U,B,I}}$ parameter previously defined. The top panels show the trend for the two high-resolution samples, while the lower panels present the medium-resolution ones. The plots disclose a clear trend: the lower the $\Delta c_{\text{U,B,I}}$, the lower the Fe abundance. We fit the data with a linear function in the form $f = ax + b$, reporting in each panel the values of both the zero point (b) and the slope (a), as well as the Spearman coefficient (r), which suggests that the correlation is significant. The four samples provide a general good agreement, in particular concerning the bright portion of the RGB where both high- and medium-resolution are present. The subsample of faint stars presents a steeper correlation. This

¹³ The difference in the absolute value of the Fe abundances between the different data sets have already been discussed in Fabrizio et al. (2012).

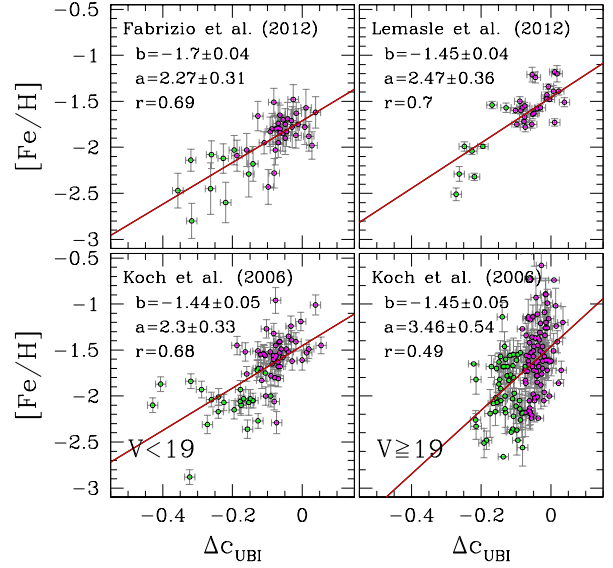


FIG. 6.— *Top* - Correlation between the $c_{\text{U,B,I}}$ colour and the iron content of stars for the high-resolution samples. *Bottom* - The same is shown also for the Koch et al. (2006) sample. The slope of the relation changes according to the luminosity of the sample. See text for details. Green and magenta symbols indicate stars with $c_{\text{U,B,I}} < -1.70$ mag and $c_{\text{U,B,I}} > -1.70$ mag, respectively, as in Fig. 5 and Fig. 6.

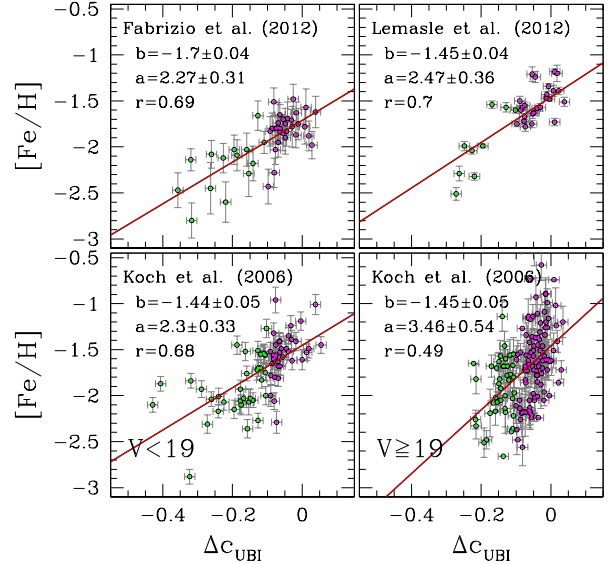


FIG. 7.— Same as Fig. 6, but in this case green and magenta symbols show stars with $\Delta c_{\text{U,B,I}} < -0.1$ mag and $\Delta c_{\text{U,B,I}} > -0.1$ mag, respectively. The plot demonstrates that the selection criterium does not affect the derived conclusions.

can be easily explained taking into account that the RGB morphology in the $c_{\text{U,B,I}}$ plane changes as a function of magnitude. In the upper part the two RGB sequences, where most of the high-resolution stars are, tend to diverge. This pushes the stars on the old RGB to lower $c_{\text{U,B,I}}$, making the relation less steep. For magnitude fainter than $V \sim 19$ mag, the two RGB are closer, and this reflects in a steeper relation between Fe and $\Delta c_{\text{U,B,I}}$.

In §2.1 we mentioned that the cut at $c_{\text{U,B,I}} = -1.70$ mag to split the old and the intermediate-age is approximately equivalent to a cut at $\Delta c_{\text{U,B,I}} = -0.1$

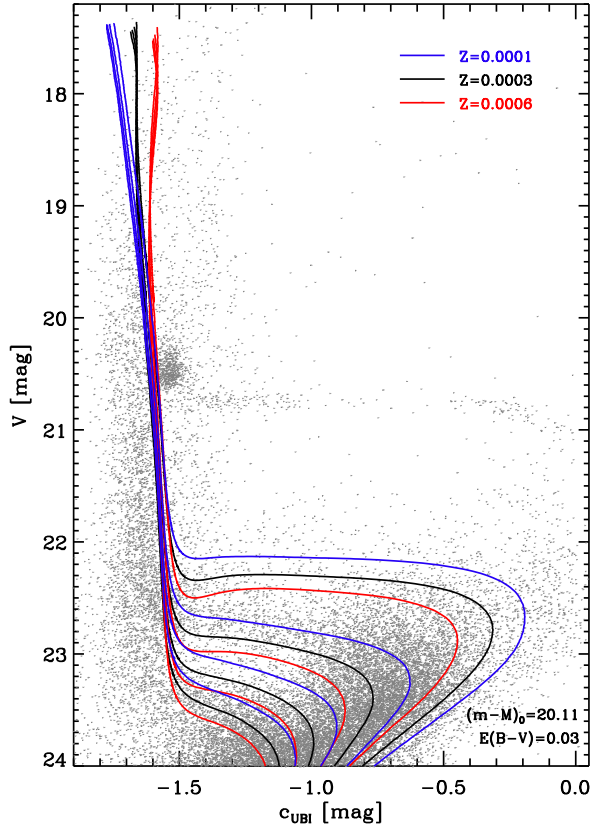


FIG. 8.— Comparison with theoretical isochrones from the BaSTI database in the $(M_V, c_{U,B,I})$ plane. For the three metallicity labeled, isochrones with age between 4 and 13 Gyr, in steps of 3 Gyr, are plotted.

mag. The anonymous referee noted that the two quoted cuts are equivalent for the high-resolution sample by Lemasle et al. (2012) (top right panel of Fig. 6) and for the faint medium-resolution sample (bottom right panel of Fig. 6). On the other hand, there are objects in the bright magnitude sample and in the high-resolution sample by Fabrizio et al. (2012) (left panels of Fig. 6) moving across the boundary of the $\Delta c_{U,B,I}$ distribution. To take account of the role that the selection criterium has on the correlation between the $\Delta c_{U,B,I}$ parameter and the iron abundance we performed the same test cutting the two populations at $\Delta c_{U,B,I} = -0.1$ mag. Data plotted in Fig. 7 show that only a few stars near the edge are classified in a different population. Therefore, this means that we cannot reach a firm conclusion concerning the nature (old v_s intermediate-age) of the objects that located across the boundary ($c_{U,B,I} = -1.70$ mag, $\Delta c_{U,B,I} = -0.1$ mag) adopted to split the two main populations. However, the above results further support the evidence that the correlation is marginally dependent on the criterium adopted to split the two populations.

Finally, we stress that this analysis is not meant to find an absolute calibration of the $c_{U,B,I}$ index as a function of metallicity. Nevertheless, the correlation supports the connection between the $c_{U,B,I}$ index and the Fe content of the Carina RGB stars.

3. DISCUSSION: STELLAR POPULATIONS AND CHEMICAL EVOLUTION IN CARINA

3.1. Comparison with theoretical models

To assess whether the theoretical models are able to reproduce the observed colour distribution of RGB stars, in the following we perform a comparison with theoretical models from the BaSTI¹⁴ database (Pietrinferni et al. 2004). Figure 8 shows a comparison in the $(V, c_{U,B,I})$ plane with scaled-solar isochrones of three different metallicities ($Z=0.0001, 0.0003, 0.0006$), and age ranging from 4 to 13 Gyr, in steps of 3 Gyr. The figure discloses that the colour range covered by the selected isochrones (≈ 0.03 mag at $V = 21$ mag) is significantly smaller than the observed one in the $(V, c_{U,B,I})$ plane. Interestingly, in the upper part of the RGB ($V \lesssim 19.5$ mag) the effect of metallicity is to split the isochrones, in agreement with the observed increasing separation of the Carina RGB sequences, discussed in Figure 1. For fainter magnitudes, it is not possible to disentangle the isochrones of different metallicity, at least in the range typical of the Carina Fe content. The effect of age along the RGB is largely negligible in this plane for both the old and the intermediate-age population. Overall, we conclude that current models based on a standard heavy-element distribution do not account for the spread in $c_{U,B,I}$ observed in the Carina RGBs.

These results do not substantially change when using α - or He-enhanced models (see also Cassisi et al. 2013a,b). Current theoretical framework does not allow us to fully explain the behaviour of the two sequences in the $c_{U,B,I}$ plane by accounting for iron, age, α -elements, and He differences alone. We remark that this cannot be due to a residual shortcoming in the adopted colour- T_{eff} transformations because we are using model predictions in a strictly differential way.

3.2. Comparison with GCs

Figure 9 shows how stars of the two sequences distribute in different CMDs, namely the $U-I, B-I, V-I$ (top row, from left to right). The two sequences appear overlapped and mixed, and therefore indistinguishable, in $B-I$, while they are slightly segregated in $V-I$ and substantially more so in $U-I$. However, the two sequences are swapped in the two planes: in $U-I$ the green symbols (old stars) are concentrated on the blue edge of the RGB, while the magenta circles (intermediate-age population) are located closer to the red edge. The opposite occurs for the $V-I$ colour. This is evident in the lower panels, where we show the fiducial lines of the two samples. To quantify the split we calculate the colour difference at magnitude level $I=20$ mag—that is, roughly two magnitudes below the tip of the RGB. As expected, we find that the separation is negligible in $B-I$, and only slightly larger in $V-I$, on the order of 0.01 mag, which is statistically significant given the typical photometric error at this magnitude level. The largest separation is found in the $U-I$ colour, of the order of -0.08 mag.

It is instructive to compare the behaviour of the RGBs in Carina with similar observations of multiple RGBs in GCs. In several GCs, the RGB and the MS of first-population stars is redder than the second-population

¹⁴ <http://basti.oa-teramo.inaf.it/index.html>

TABLE 1
MEAN METALLICITIES FOR THE DIFFERENT SPECTROSCOPIC SAMPLES AND STELLAR POPULATIONS

| Spectroscopic sample | $\langle [\text{Fe}/\text{H}] \rangle_{\text{old}}$ | σ | N_{stars} | $\langle [\text{Fe}/\text{H}] \rangle_{\text{int}}$ | σ | N_{stars} |
|---|---|----------|--------------------|---|----------|--------------------|
| <i>Cut at $c_{\text{U,B,I}} = -1.70 \text{ mag}$</i> | | | | | | |
| Fabrizio et al. (2012) | -2.32 ± 0.08 | 0.25 | 10 | -1.82 ± 0.03 | 0.20 | 34 |
| Lemasle et al. (2012) | -2.03 ± 0.13 | 0.35 | 8 | -1.52 ± 0.03 | 0.18 | 27 |
| Koch et al. (2006) [$V < 19 \text{ mag}$] | -2.06 ± 0.05 | 0.24 | 24 | -1.55 ± 0.03 | 0.24 | 47 |
| Koch et al. (2006) [$V \geq 19 \text{ mag}$] | -1.96 ± 0.05 | 0.33 | 54 | -1.56 ± 0.04 | 0.38 | 87 |
| <i>Cut at $c_{\text{U,B,I}} = -1.67 \text{ mag}$</i> | | | | | | |
| Fabrizio et al. (2012) | -2.25 ± 0.07 | 0.27 | 14 | -1.79 ± 0.03 | 0.16 | 30 |
| Lemasle et al. (2012) | -1.80 ± 0.10 | 0.37 | 15 | -1.51 ± 0.04 | 0.18 | 20 |
| Koch et al. (2006) [$V < 19 \text{ mag}$] | -1.92 ± 0.06 | 0.34 | 36 | -1.52 ± 0.03 | 0.19 | 35 |
| Koch et al. (2006) [$V \geq 19 \text{ mag}$] | -1.85 ± 0.04 | 0.38 | 86 | -1.50 ± 0.05 | 0.41 | 55 |
| <i>Cut at $c_{\text{U,B,I}} = -1.73 \text{ mag}$</i> | | | | | | |
| Fabrizio et al. (2012) | -2.34 ± 0.11 | 0.28 | 8 | -1.85 ± 0.04 | 0.21 | 36 |
| Lemasle et al. (2012) | -2.10 ± 0.13 | 0.31 | 7 | -1.52 ± 0.03 | 0.17 | 28 |
| Koch et al. (2006) [$V < 19 \text{ mag}$] | -2.10 ± 0.06 | 0.25 | 18 | -1.59 ± 0.04 | 0.26 | 53 |
| Koch et al. (2006) [$V \geq 19 \text{ mag}$] | -1.93 ± 0.05 | 0.33 | 38 | -1.63 ± 0.04 | 0.41 | 103 |

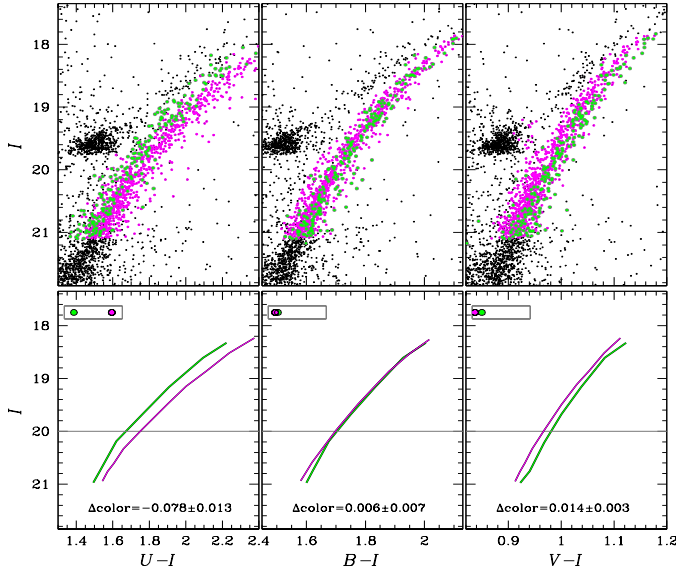


FIG. 9.— *Top* - I versus $U-I$, $B-I$, $V-I$ CMDs zoomed in the RGB region, with stars from the two RGB selected in the $\Delta c_{\text{U,B,I}}$ are highlighted in green (old population) and magenta (intermediate-age). *Bottom* - Ridge lines of the two populations. Note the change in the relative position for decreasing colour baseline. The mean colour difference with respect of the colour line at magnitude $I = 20 \text{ mag}$ is labeled, and illustrated by the coloured points on the top-left corner of each panel.

RGB and MS in $B-I$, and $V-I$ colours, and the colour separation increases for increasing colour baseline (that is, $\Delta(B-I) > \Delta(V-I) > 0$). However, the RGBs can merge together or even change their relative positions when using a near-UV filter ($\Delta(U-I) < 0$). On the other hand, if far-ultraviolet (FUV) filters are adopted the separation between the two RGBs increases again and is significantly larger in $FUV - I$ than in visual colours (see Milone et al. 2012c,a).

This has been explained as due to the detailed abundances of the various light elements (e.g., C, N, Na, O) and Helium. In particular, the colours of the first-generation stars in GCs are well reproduced assuming primordial He abundance and an O-rich/N-poor composition that is similar to that of halo-field stars of the same

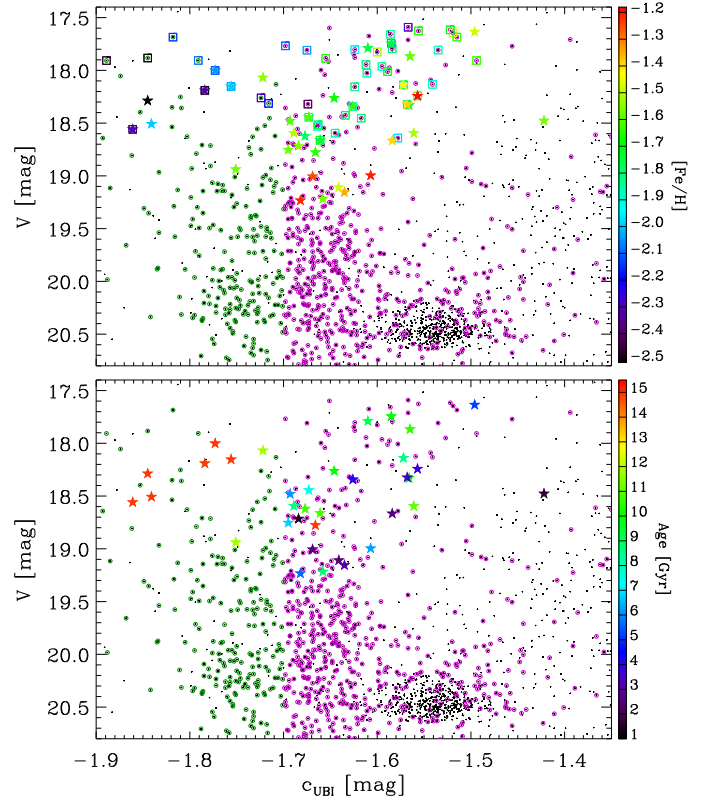


FIG. 10.— $V-c_{\text{U,B,I}}$ diagram for bright Carina stars. The green and magenta circles show the separation at $c_{\text{U,B,I}} = -1.70 \text{ mag}$ performed in Fig. 6. The starred symbols highlight the 35 stars from Lemasle et al. (2012). The colour code used for these symbols, reproduced on the right of both panels, displays the iron content (top) and age (bottom) determined by Lemasle et al. (2012).

metallicity. On the other hand, the colours of the second-population stars agree with a composition in which N and Na are enhanced—along with increased He—while C and O are depleted. Sbordone et al. (2011) have demonstrated that such abundance variations mostly affect the CN- NH- CH-bands in the UV part of the spectrum, and this translates into different colours for the different pop-

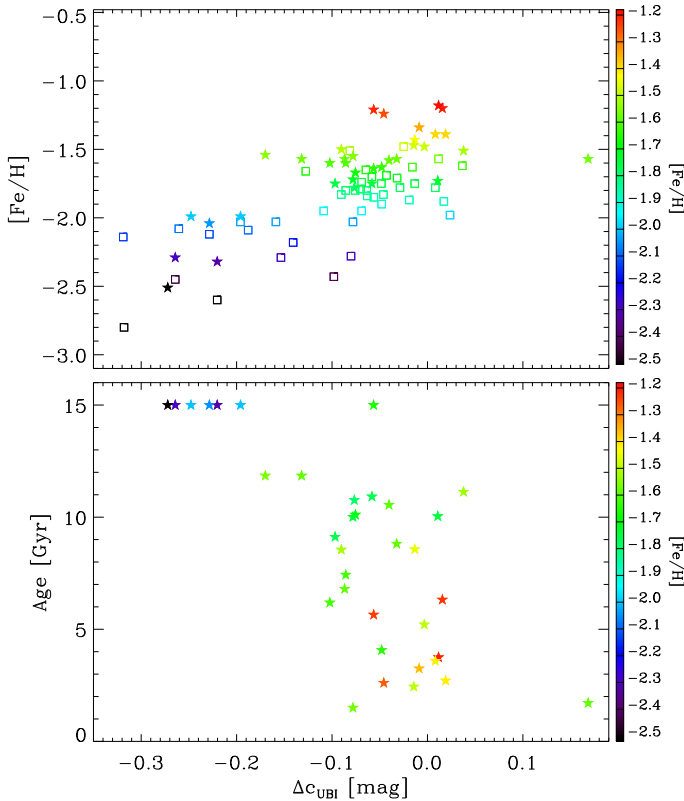


FIG. 11.— Iron abundance (top panel) and age (bottom) from Lemasle et al. (2012) as a function of the $\Delta c_{U,B,I}$ index. The colour code used in both panel accounts for the metallicity of the 35 stars, and is the same used in the top panel of Fig. 10. The error bars accounts for the photometric error of our photometry and the uncertainties provided by Lemasle et al. (2012) on their age and metallicity determinations.

ulations when the UV filters are used. These effects can be well reproduced by stellar models if the appropriate chemical mixtures are adopted (Sbordone et al. 2011).

Results shown in Figure 9 demonstrate that the RGB behaviour of stellar populations in the Carina dSph and in GCs differ significantly. Carina is indeed an intrinsically more complicated system than a typical GC, due to the bursty star-formation history and the large age and metallicity spread present in each population. Multiple populations in a GC formed on a much shorter time-scale, and, in most cases, the internal chemical enrichment affected only the light elements involved in the high temperature H burning processes, while typically no spread in iron, due to Supernova pollution, is found.

Moving to a more speculative scenario, a possible explanation for the empirical evidence is that light-element abundances could play a non-negligible role in determining the behaviour of the multiple RGBs in the Carina dSph, in analogy to what is observed in GCs. The $c_{U,B,I}$ index is very sensitive to light-element variations, which are measured in dwarf galaxies as well. However, it is not clear at present whether the chemical pattern are similar to that of GCs. In fact, the Na-O and C-N anti-correlations have not been observed for dSph galaxies in general, or for Carina in particular. Venn et al. (2012)

report measurement of one O line and also NaI determinations for few stars, but no anti-correlation clearly stems from the data. On the other hand, more metal-poor stars, with $[Fe/H] < -2$ dex, seem to have lower Na content than more metal-rich ones (Venn et al. 2012, their Figure 12), in agreement with what found in GCs. Overall, C and N abundances are yet not available. These can be crucial elements, as the overall C+N+O abundance significantly influences the luminosity of the SGB and hence affects the age determinations of the different populations (Cassisi et al. 2008; Ventura et al. 2009; Marino et al. 2012). Measurement of the overall C+N+O content of intermediate-age and old stars in Carina is mandatory to properly estimate the age of its stellar populations and thus to properly calibrate the chemical enrichment history.

3.3. Comparison with previous results

Following the referee’s suggestion, we show in Fig. 10 a comparison with literature values, in particular the metallicity (top panel) and the age (bottom). The top panel shows the $V - c_{U,B,I}$ diagram, with highlighted in green and magenta the two groups of stars selected in §2.2. The starred symbols show the 35 stars by Lemasle et al. (2012), while the squares the 44 stars by Fabrizio et al. (11 objects in common 2012) colour-coded as labeled. The above data indicate that the most metal-poor stars attain the lowest $c_{U,B,I}$ values, and fall on the RGB sequence identified by the green circles. On the other hand, stars more metal-rich than $[Fe/H] \sim -2$, attain larger $c_{U,B,I}$ values, and all but three fall on the other sequence identified by the magenta circles.

The bottom panel of Fig. 10 shows once again the two groups of stars selected in §2.2 in green and in magenta together with the 35 stars by Lemasle et al. (2012). The spectroscopic sample by Fabrizio et al. (2012) was not plotted in this panel, because the authors did not provide an individual age estimate. Interestingly, we found that the most metal-poor stars also have the largest age (saturated at 15 Gyr). This implies that all but one of these objects are located in the lowest $c_{U,B,I}$ sequence, which we identify with the RGB of the old population. Similarly, all the intermediate-age stars ($t < 8$ Gyr) cluster in the region of the higher $c_{U,B,I}$ stars. On the other hand, starred symbols plotted with greenish colour, with estimated ages between ~ 8 and ~ 11 Gyr, attain a $c_{U,B,I}$ index ranging from ~ -1.75 to ~ -1.42 mag. In this context it is worth mentioning that the current comparison does not allow us to reach a firm conclusion concerning the objects with ages ranging from 8 to 11 Gyrs. The reasons are manifold. The uncertainty associated to the individual ages of RG stars is at least of the order of 2 Gyr (Lemasle et al. 2012). The uncertainty on the individual iron abundance is at least of the order of 0.1 dex (Fabrizio et al. 2012). The sample is limited and these objects are located across the boundary adopted to split the old and the intermediate-age population.

Fig. 11 shows the same $[Fe/H]$ abundance (top) and age (bottom) as a function of the $\Delta c_{U,B,I}$ index, with the same colour code adopted for metallicity in the top panel of in Fig. 10. The above figures suggest a segregation, in the sense that stars with more negative $\Delta c_{U,B,I}$ are systematically older and more metal-poor than those with higher index. This further strengthens the use of $c_{U,B,I}$

and $\Delta_{\text{C},\text{B},\text{I}}$ to separate stars from different populations. However, this result should be cautiously treated, since other parameters together with age and iron content are necessary to fully characterize the properties of the Carina stars (see Fig. 8 and §3.2). This means that the comparison between isochrones and CMD along the RGB might be affected by possible systematic effects. The anonymous referee noted that the correlation between age and metallicity is a thorny problem of the Carina dSph, since the two main episodes of star formation show a well defined separation of the order of 3-4 Gyrs. According to the recent literature, the age distribution of the two main stellar population in Carina cover a broad range in age (Mighell 1990; Smecker-Hane et al. 1994, 1996; Mighell 1997; Hurley-Keller et al. 1998; Hernandez et al. 2000; Dolphin 2002; Rizzi et al. 2003; Monelli et al. 2003; Bono et al. 2010; Stetson et al. 2011; Lemasle et al. 2012). The difference is mainly due to the adopted stellar isochrones and to the diagnostic adopted to constrain the age (MSTO v_s red giants). Unfortunately, we still lack firm theoretical and empirical constraints to assess whether the Carina star formation episodes were affected by the interaction with the Galaxy (Monelli et al. 2003; Pasetto et al. 2011; Fabrizio et al. 2011; Lemasle et al. 2012) However, the above uncertainties do not affect our conclusions, since we are only using relative ages to separate the old and the intermediate-age stellar populations.

The quoted problems do not apply to the other satellite dSphs, such as Sculptor, showing a well defined age-metallicity relation (de Boer et al. 2012; Starkenburg et al. 2013). This stellar system appears as a fundamental benchmark to further constrain the use of the $c_{\text{U},\text{B},\text{I}}$ index to identify distinct stellar populations.

4. CONCLUSIONS

In this paper we have investigated the stellar populations in Carina adopting an observational approach that has been successfully used to study multiple populations in GCs. The main results can be summarized as follows:

- The use of the $c_{\text{U},\text{B},\text{I}}$ pseudo-colour allows the discrimination between old and intermediate-age populations. The new purely photometric diagnostic allows us in breaking the severe age-metallicity degeneracy along a significant portion of the RGB of this stellar system. In particular, we are able to clearly follow the evolutionary sequence of the old and of the intermediate-age populations for at least three magnitudes along the RGB. This approach is fully supported by the analysis sample of bona-fide Carina stars selected according to their radial velocity.
- By comparing with published spectroscopy, we found a significant correlation between the $c_{\text{U},\text{B},\text{I}}$ index of RGB stars and their iron content. This conclusion is supported by three independent samples of spectroscopic measurements. We derive that the mean metallicity of the old population is on average 0.5 dex lower than the

intermediate-age one.

- A comparison with theoretical models demonstrates that current isochrones calculated for a standard heavy-element mixture cannot reproduce the observed distribution of stars in the (V , $c_{\text{U},\text{B},\text{I}}$) plane.
- The appearance of Carina RGBs in different CMDs significantly differs from what is observed for multiple populations within GCs.

The comparison between theoretical models and observations indicates that the RGB bimodality disclosed by $c_{\text{U},\text{B},\text{I}}$ cannot be explained on the basis of a difference in age and/or in Fe abundance only. In dealing with mono-metallic GCs, the split of the different sub-populations is currently explained as the combination of light-element (mainly C,N,O) and helium variations (e.g. Marino et al. 2008; Yong & Grundahl 2008; Sbordone et al. 2011; Milone et al. 2012c). Very likely a possible difference in C, N, O –and probably helium– between the old and young population, combined with metallicity and age effects, can be also responsible of the observed RGB bimodality in Carina. However, in the case of Carina there are no measurements for most of these elements. In addition, while in GCs C,N,O abundances are connected with well-known correlations and anticorrelations the pattern of C,N,O variation in this dwarf is largely unexplored (e.g. Venn et al. 2012) and the empirical scenario is still limited by both accuracy and statistics.

Detailed knowledge of the chemical pattern in dwarf galaxies, especially in comparison with GCs, is very important to constrain the chemical evolution in the Milky Way environment. The techniques shown here could be very promising for breaking the age-metallicity degeneracy in the CMDs of stellar systems with complex star formation history, and should be tested in different systems. In particular, comparing Carina with other galaxies having different star formation histories, such as the purely old ones (Draco, Ursa Minor, Sculptor) and those with extended star formation (Fornax, Leo I) would be particularly valuable.

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